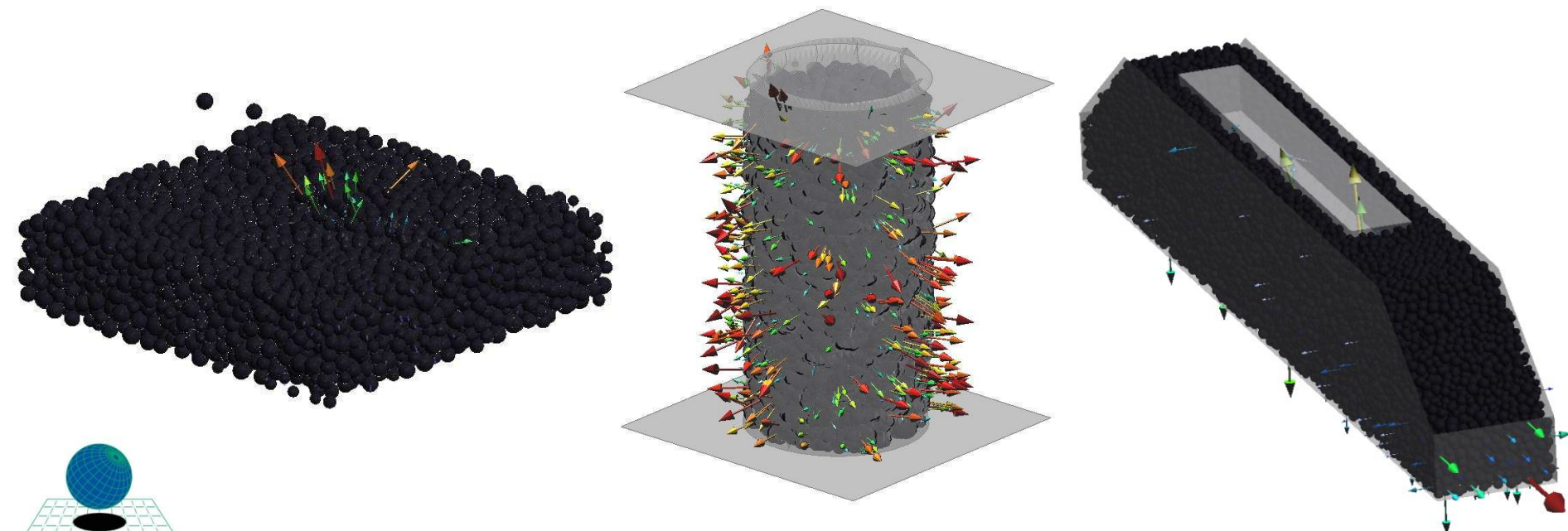


Numerical modelling of railway ballast behaviour using the Discrete Element Method (DEM) and spherical particles



OUTLINE

- Motivation and objectives

- Railway Ballast

- Discrete Element Method (DEM)

- Software

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- Ballast representation with spheric particles
- Laboratory tests
- Different particles shape
- Conclusions

MOTIVATION AND OBJECTIVES

Motivation:

- Increasing interest all over the world in high-speed trains

Objectives:

- Study railway ballast properties

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Develop a numerical tool to reproduce quantitatively the macro-mechanical behaviour of railway ballast using the DEM

- Validate the code

BALAMED

January 2013 – December 2015



GOBIERNO
DE ESPAÑA

MINISTERIO
DE ECONOMÍA
Y COMPETITIVIDAD

RAILWAY BALLAST

Layer of granular material placed under the sleepers whose roles are: resisting to vertical and horizontal loads and facing climate action

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DISCRETE ELEMENT METHOD

Contact constitutive model:

Rigid bodies, deformation concentrated in contact points

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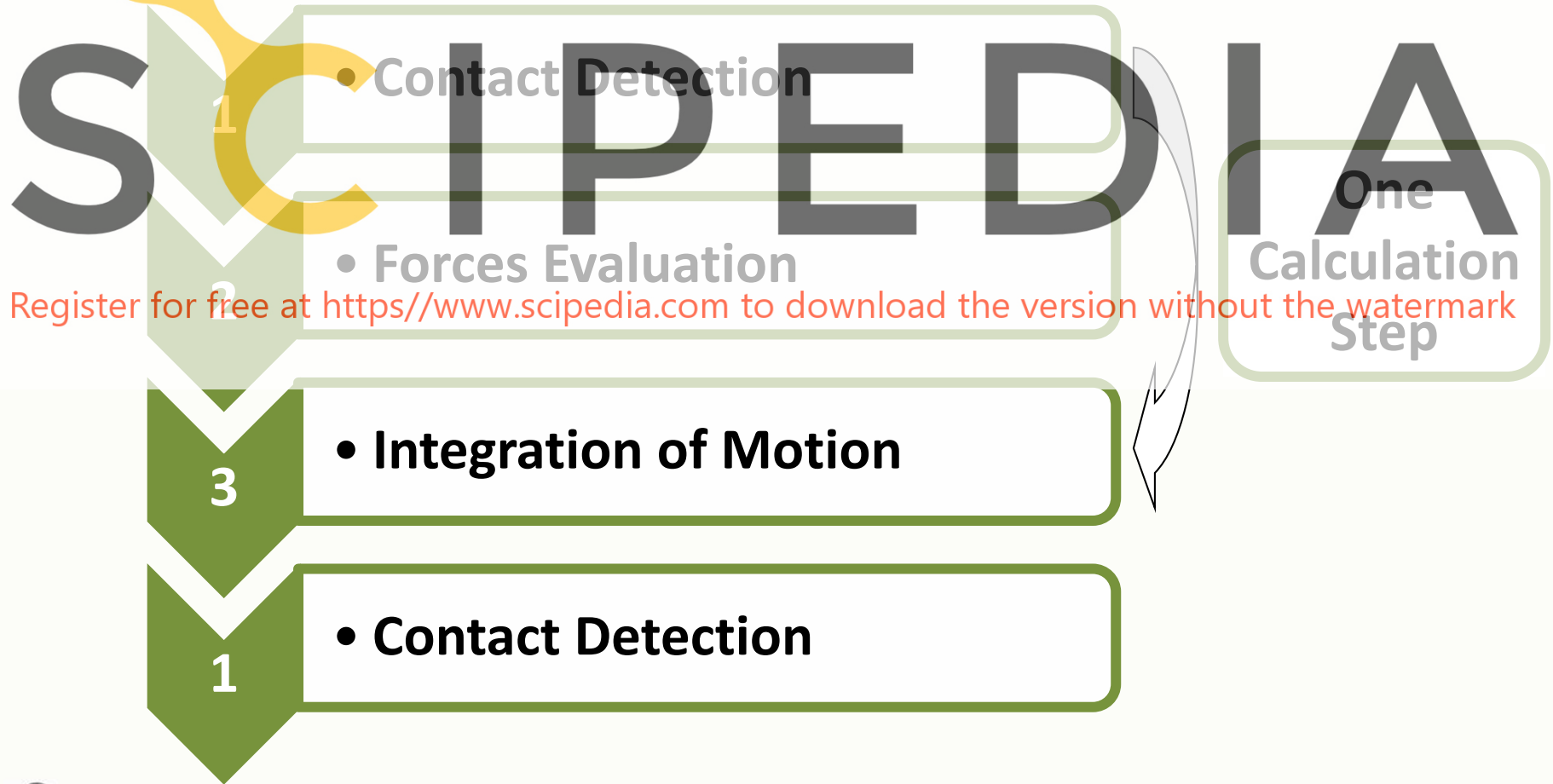
$$\begin{cases} m \cdot \ddot{u} = F \\ I \cdot \dot{\omega} = M \end{cases}$$

$$F = \sum_{c=1}^{N_c} F^c + F^{ext} + F^{damp}$$

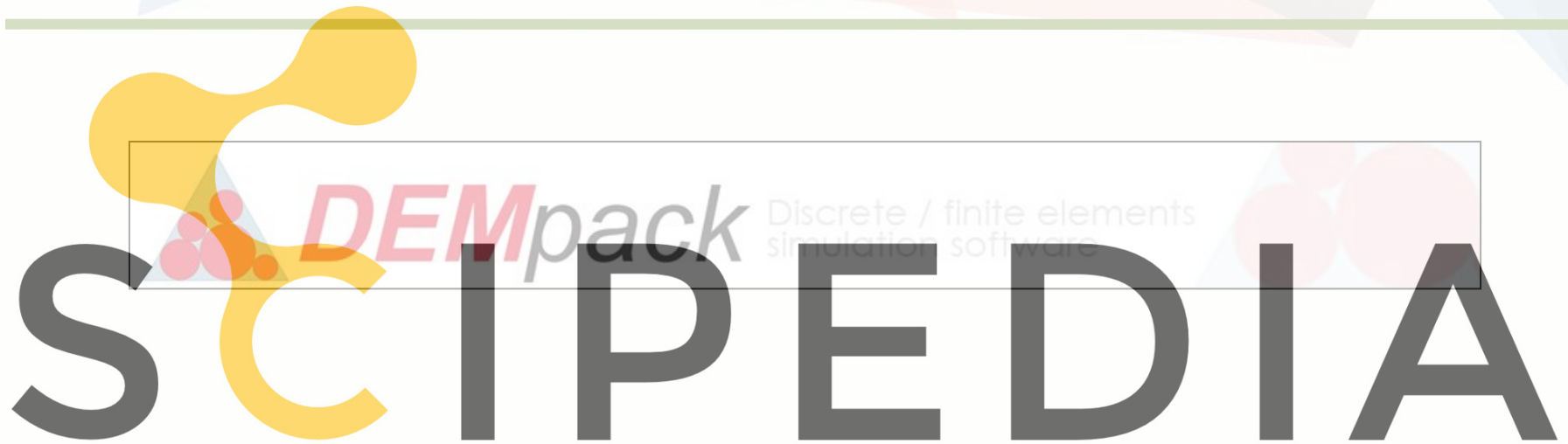
$$M = \sum_{c=1}^{N_c} (r^c \times F^c + q^c) + M^{ext} + M^{damp}$$

DISCRETE ELEMENT METHOD

Algorithm:



SOFTWARE



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<http://www.cimne.com/dem-pack/>

<http://www.cimne.com/kratos/>

<http://gid.cimne.upc.es/>

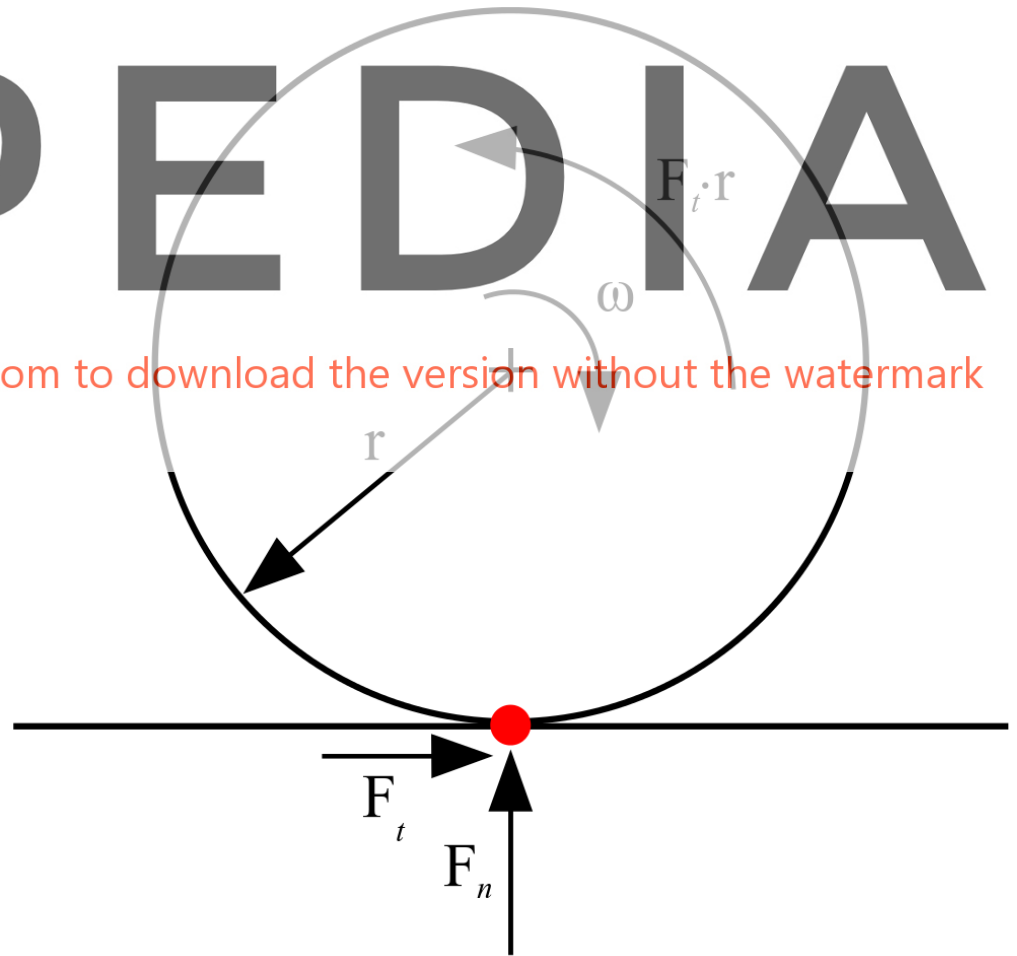
BALLAST REPRESENTATION WITH SPHERES

Rolling friction:

Geometrical “property”
that consists in
imposing a virtual
moment opposite to
particle rotation and
dependent on its size

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C. M. Wensrich and A. Katterfeld.
Rolling friction as a technique for
modelling particle shape in DEM.
Powder Technology, 217:409–417,
February 2012



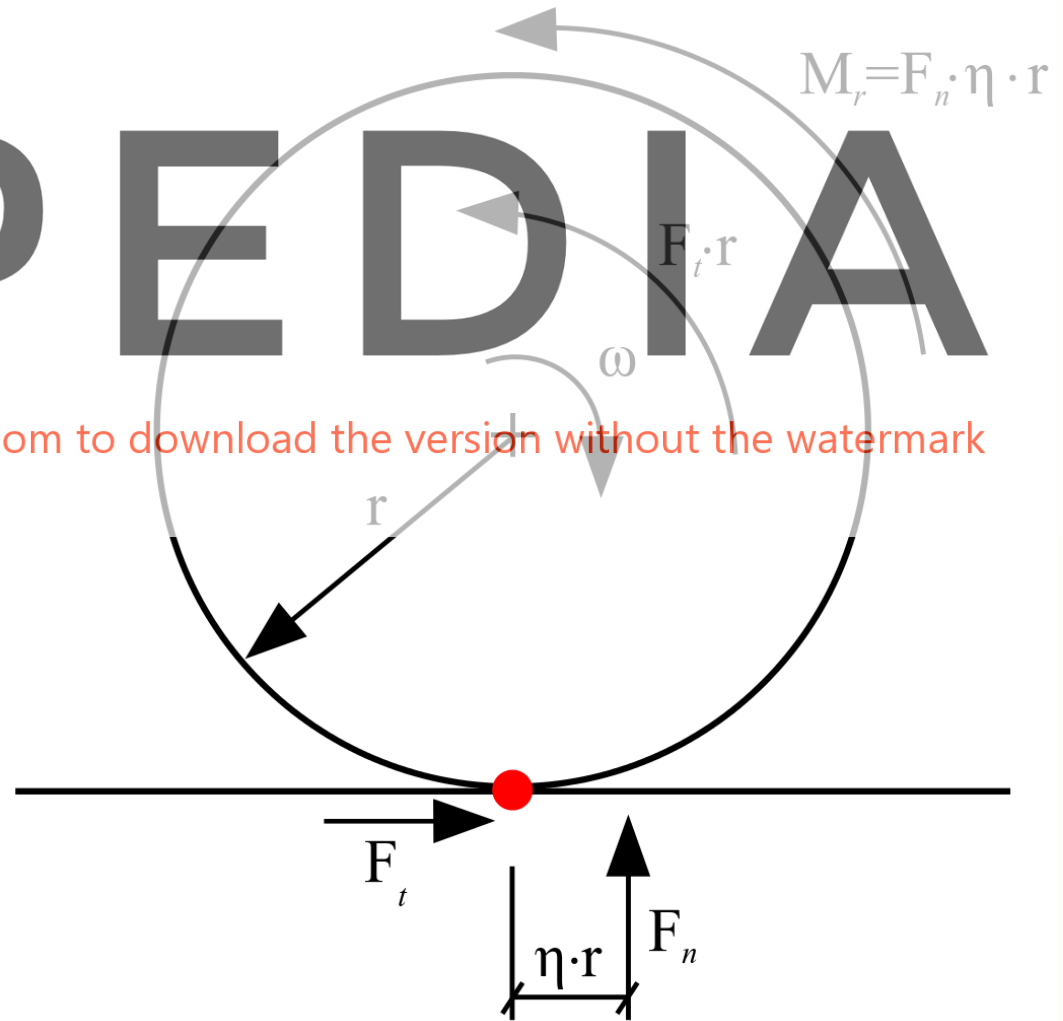
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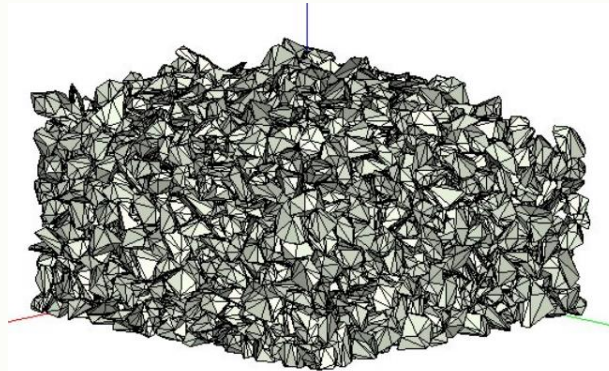
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C. M. Wensrich and A. Katterfeld.
Rolling friction as a technique for
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Powder Technology, 217:409–417,
February 2012



TEST RESULTS

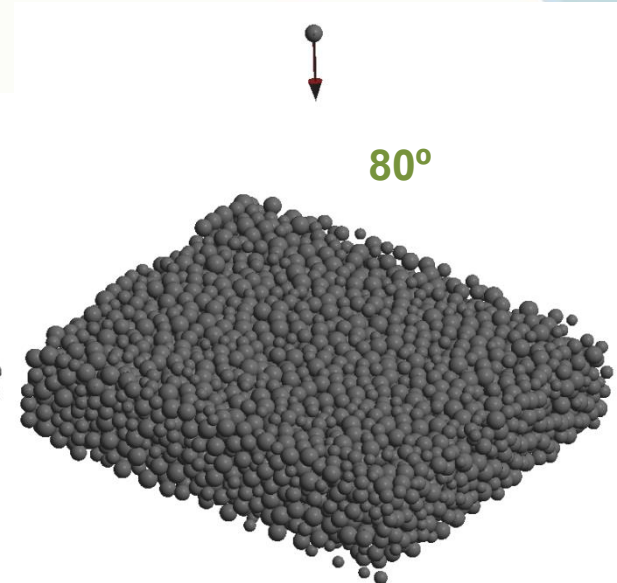
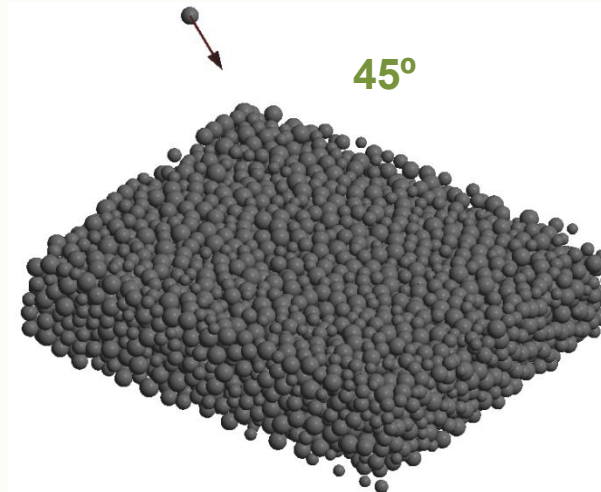
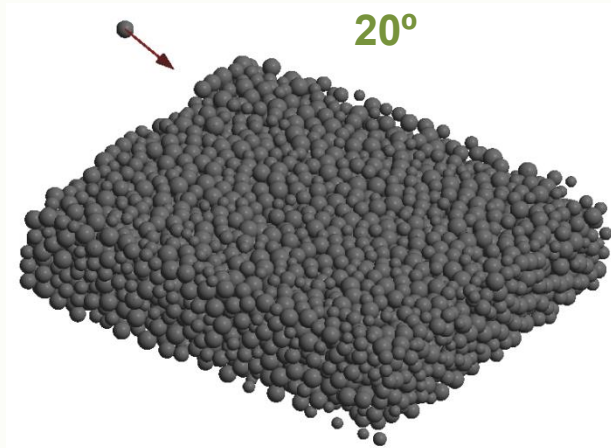
Ballast stones projection:



Kaltenbach, H.J. et al. T. Assessment of the aerodynamic loads on the trackbed causing ballast projection: results from the DEUFRAKO project aerodynamics in open air (AOA). Seoul, 2008.

TEST RESULTS

Ballast stones projection:



Ballast properties

Density (kg/m ³)	2700	Friction coeff.	0.6
Young Modulus (Pa)	1.2e8	Restitution coeff.	0.4
Poisson ratio	0.18	Rolling friction coeff.	0.33
Mean diameter (m)	0.05		

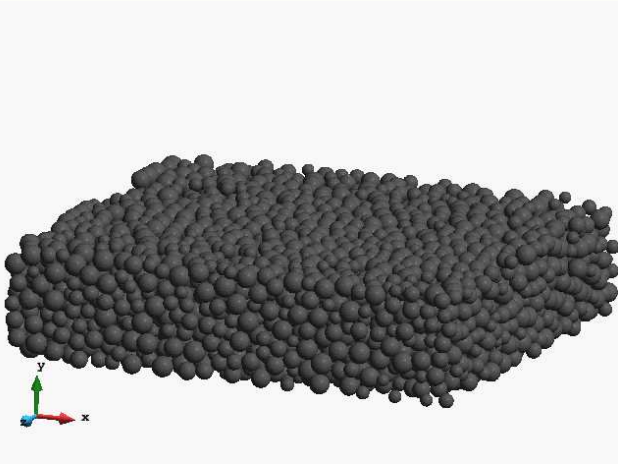
Input parameters

Projected stone radius (m)	0.05
----------------------------	------

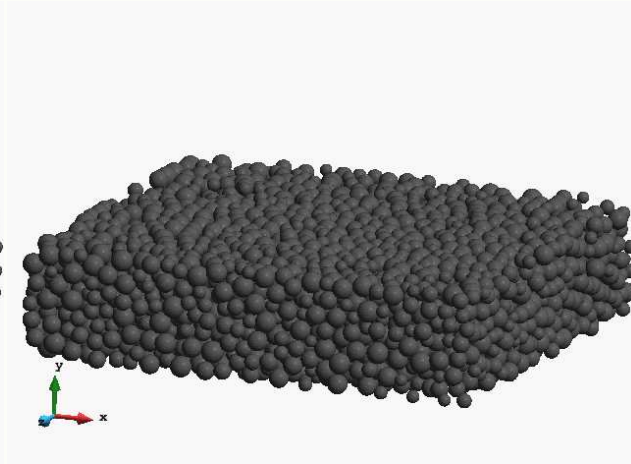
TEST RESULTS

Ballast stones projection:

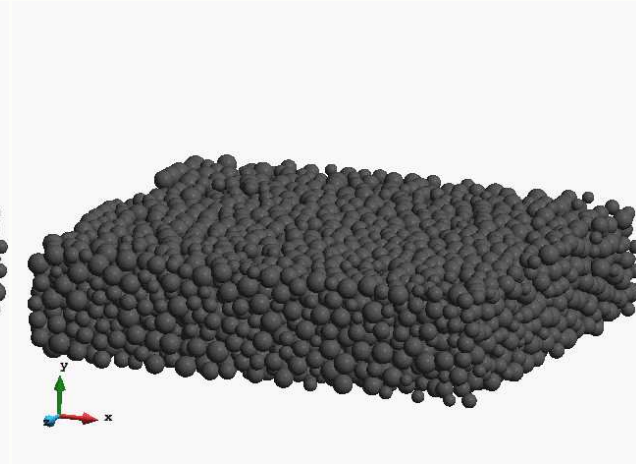
1000 J



20°



45°

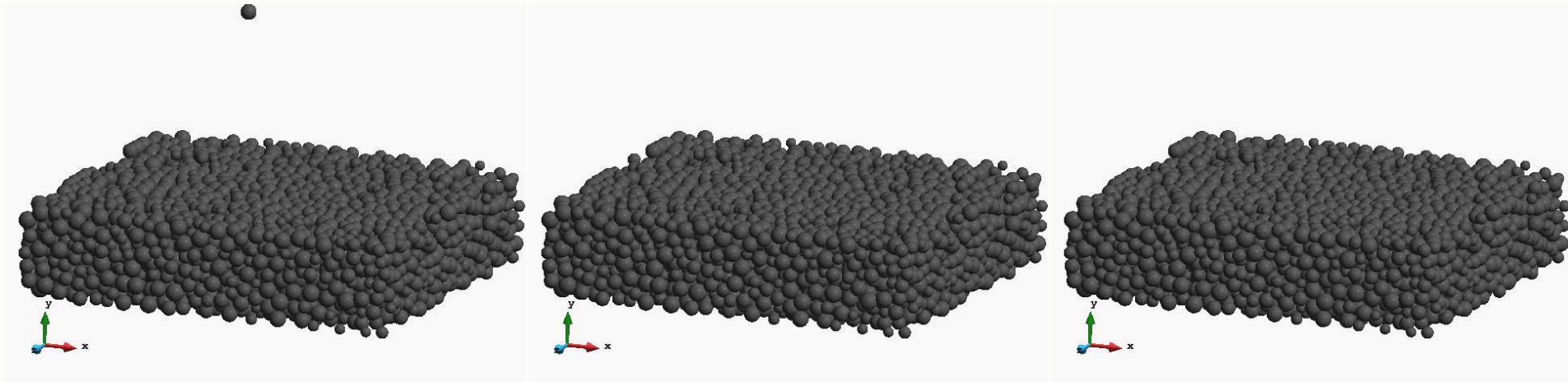


80°

TEST RESULTS

Ballast stones projection:

80°



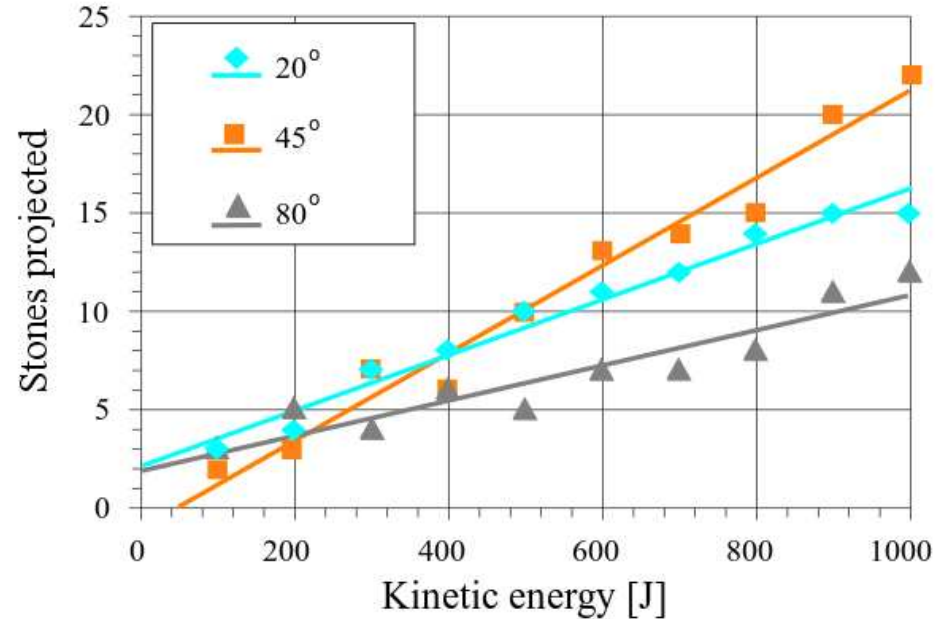
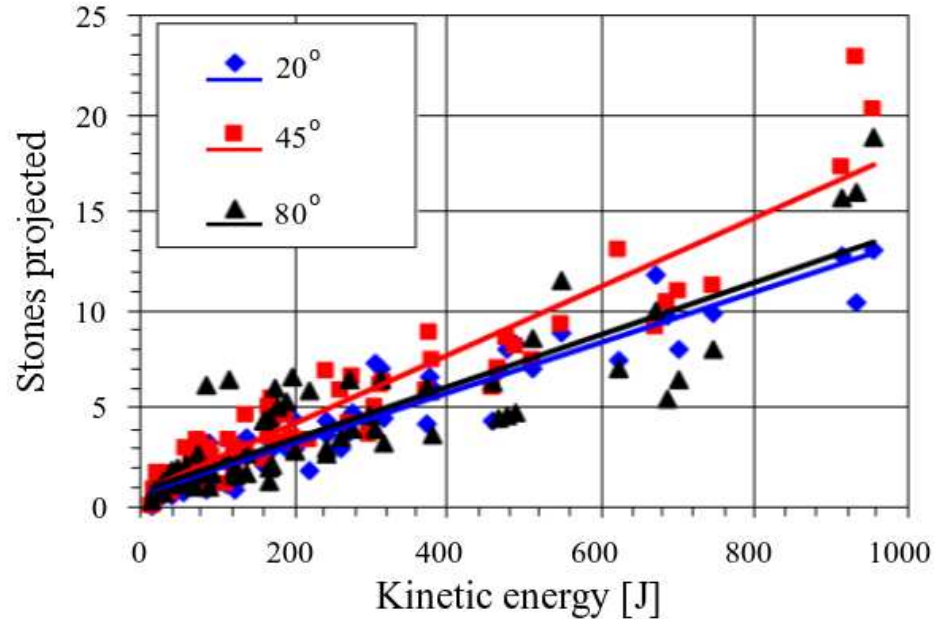
100 J

500 J

1000 J

TEST RESULTS

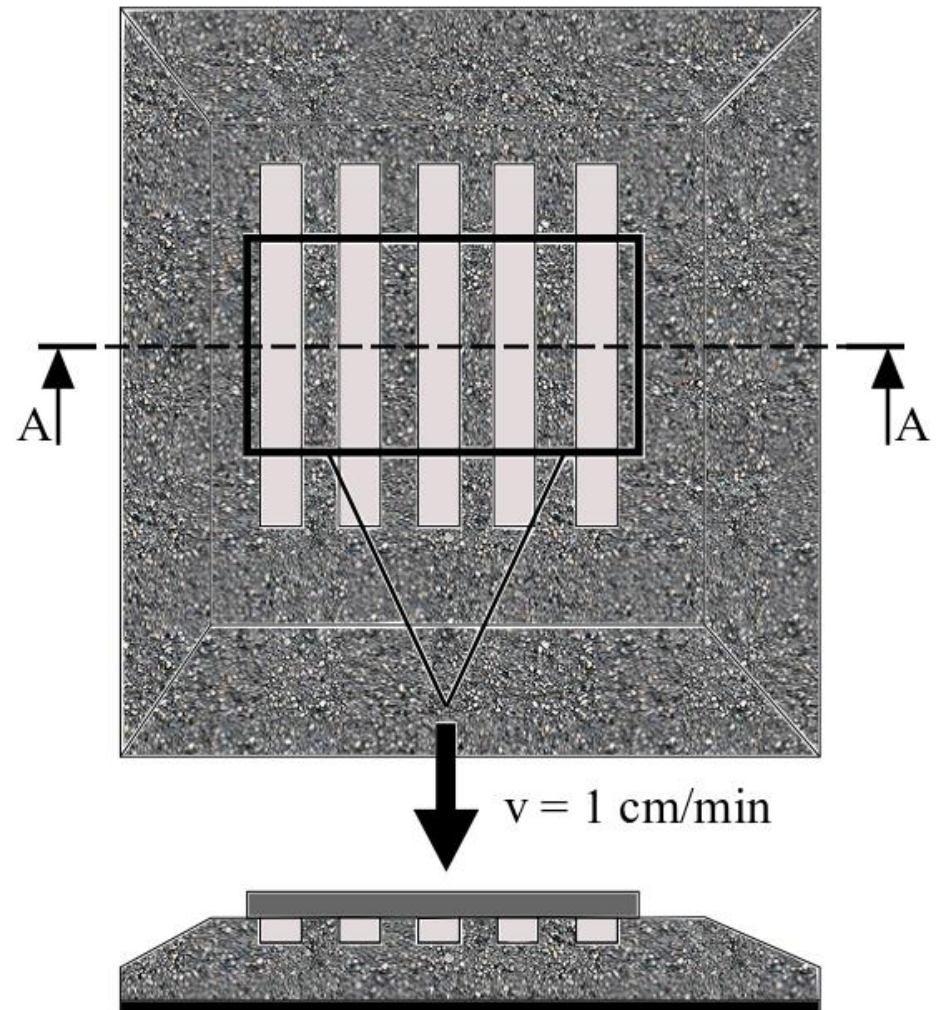
Ballast stones projection:



TEST RESULTS

Lateral resistance test:

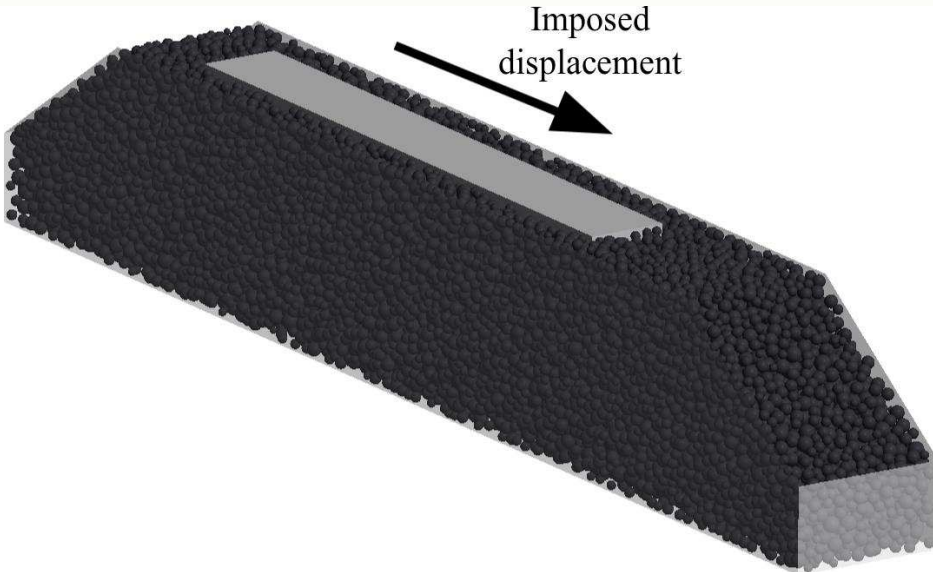
Vertical load= 0 N
Sleepers Velocity = 0.0001667 m/s



Zand and Moraal (1997)
Roads and Railways Research Laboratory
Technical University of Delft

TEST RESULTS

Lateral resistance test:



Ballast properties

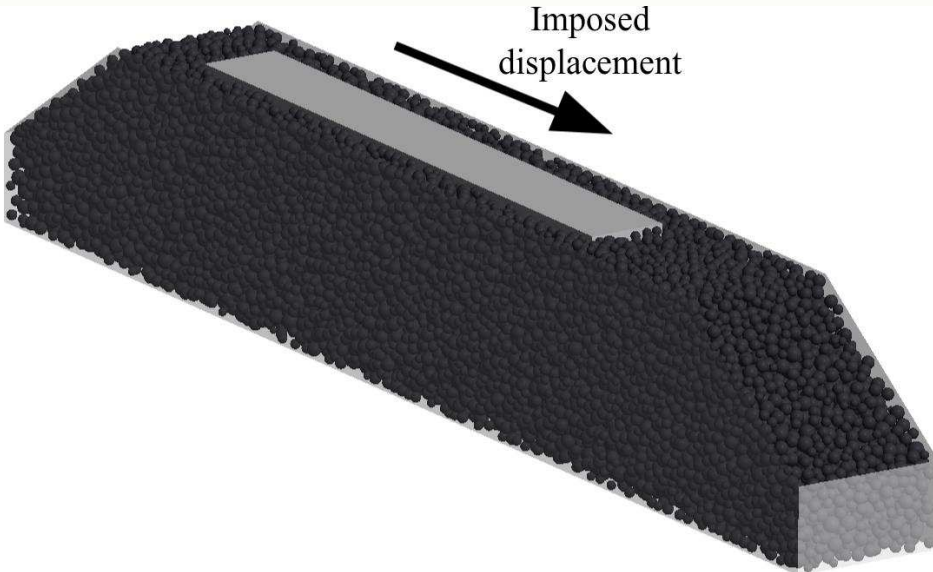
Density (kg/m^3)	2700
Young Modulus (Pa)	5.1e9
Poisson ratio	0.18
Mean diameter (m)	0.05
Friction coeff.	0.6
Friction coeff. ballast/sleeper	0.7
Restitution coeff.	0.4
Rolling friction coeff.	0.33

Input parameters

Stabilization time (s)	1.0
------------------------	-----

TEST RESULTS

Lateral resistance test:



Ballast properties

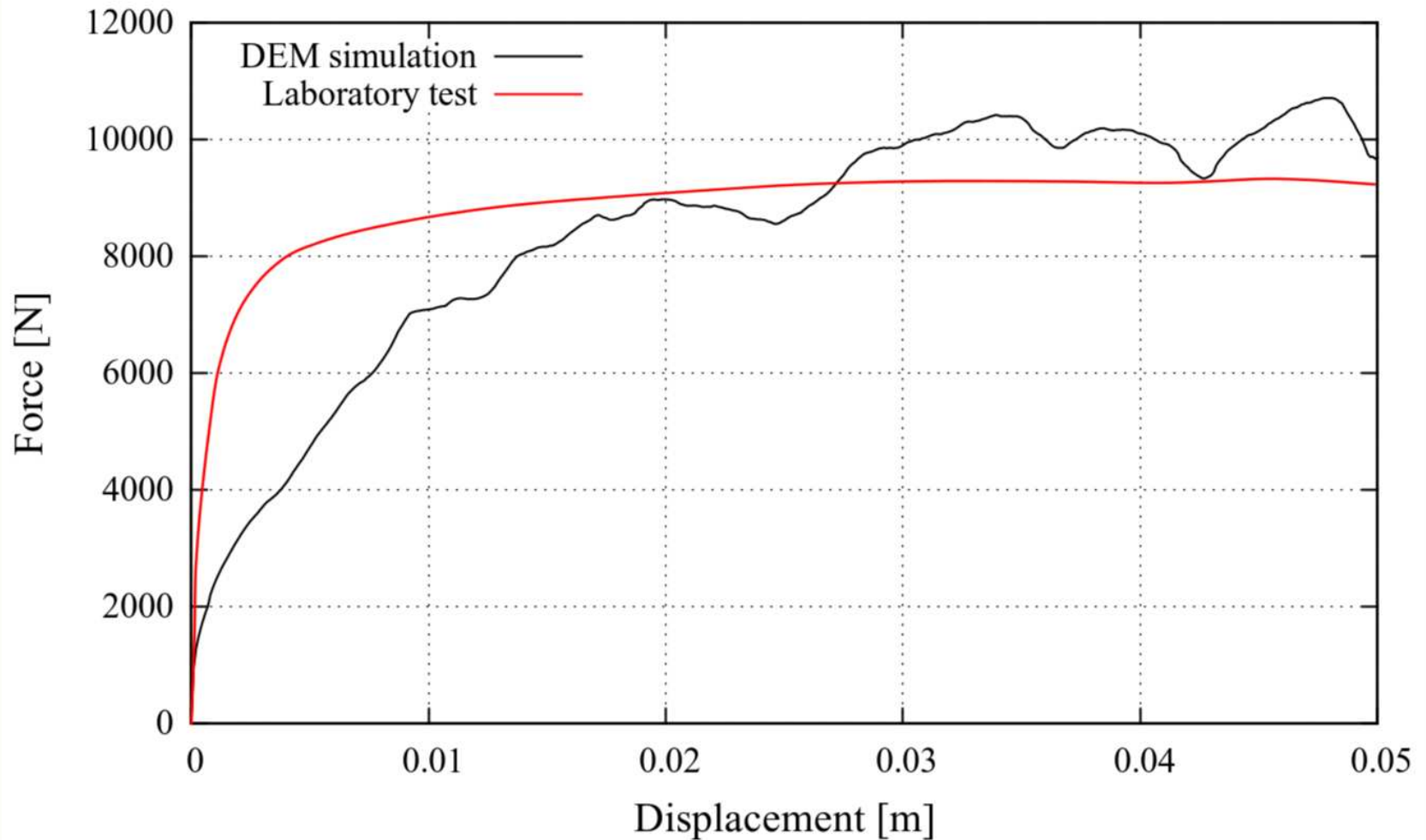
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TEST RESULTS

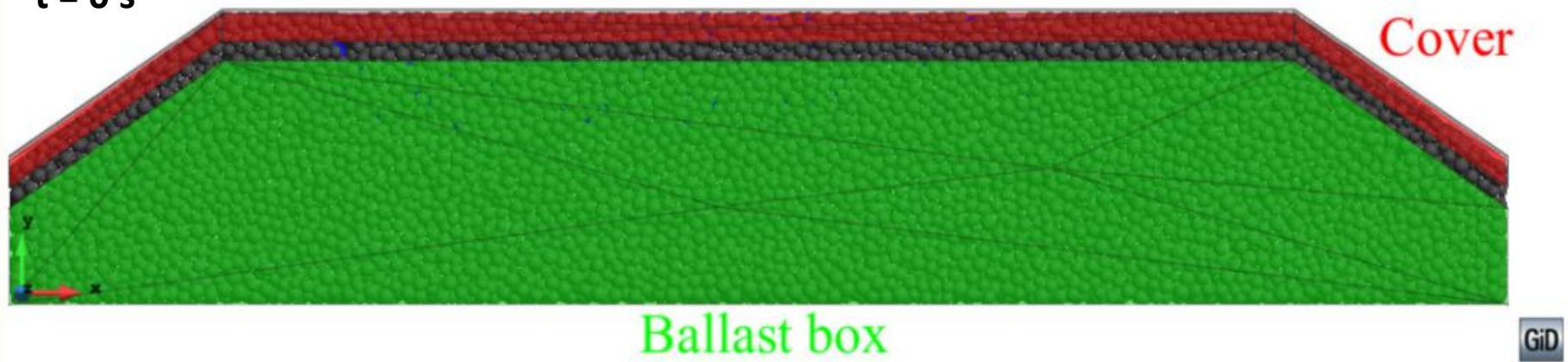
Lateral resistance test:



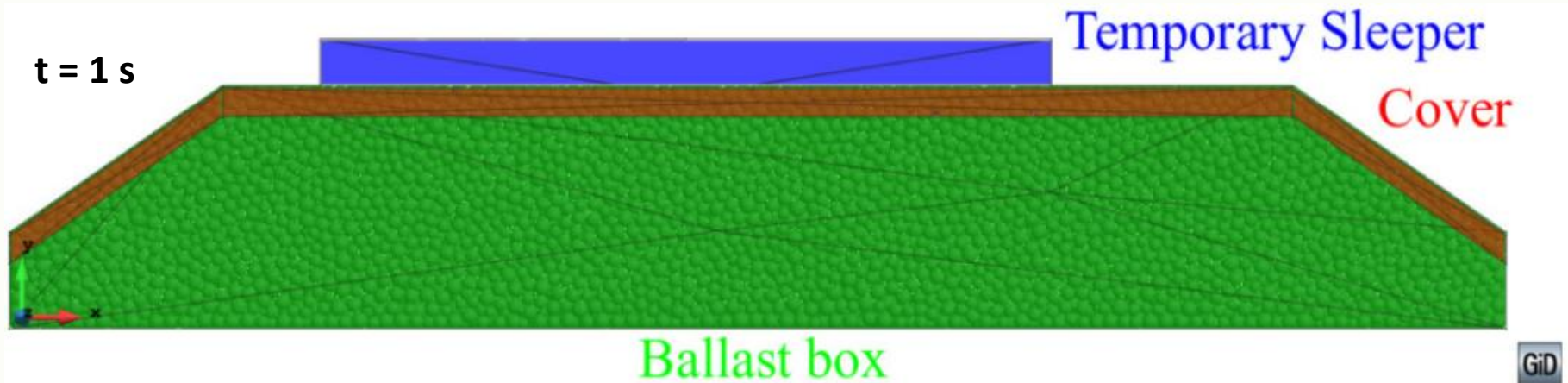
TEST RESULTS

Lateral resistance test:

$t = 0$ s

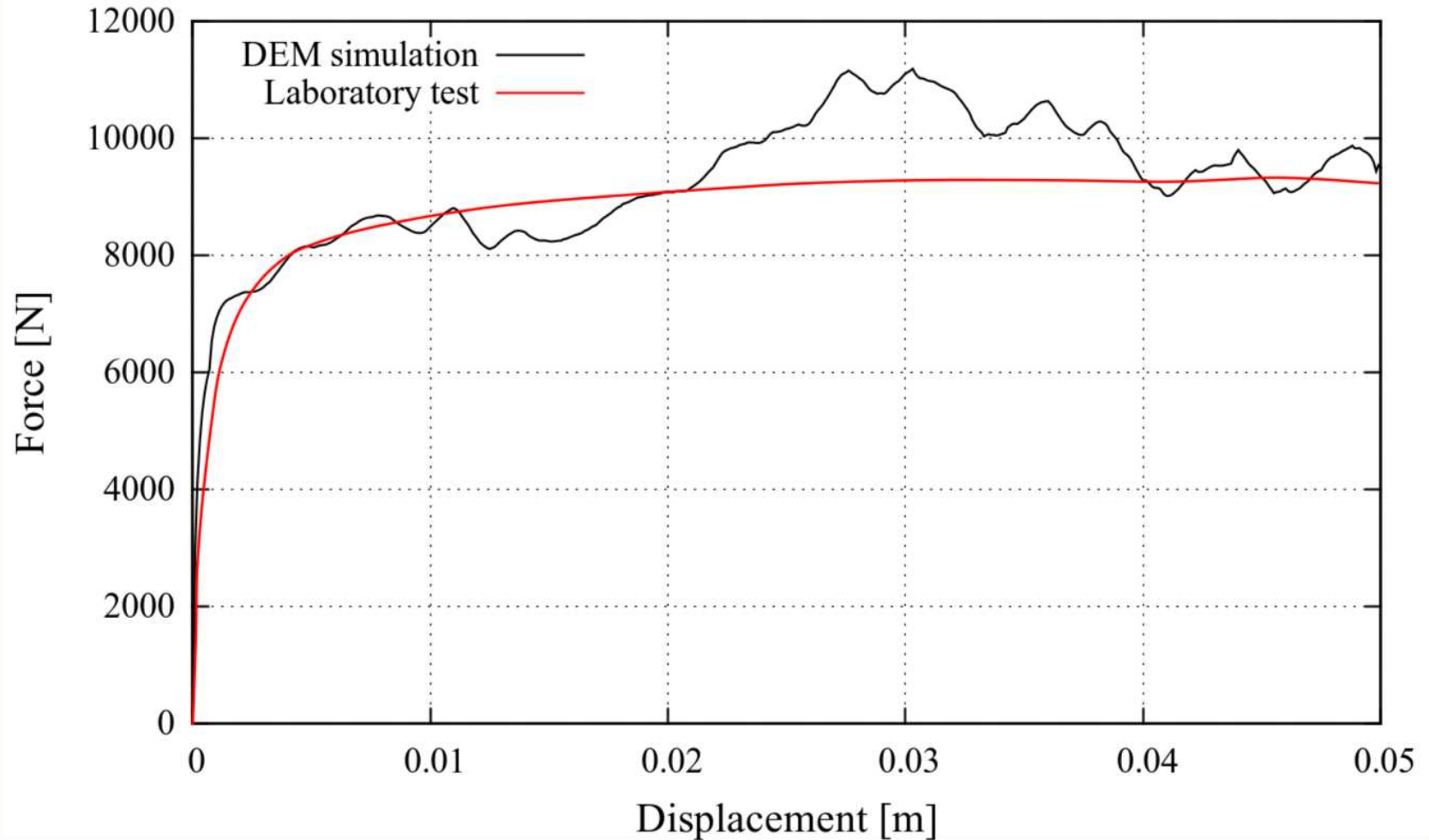


$t = 1$ s



TEST RESULTS

Lateral resistance test:



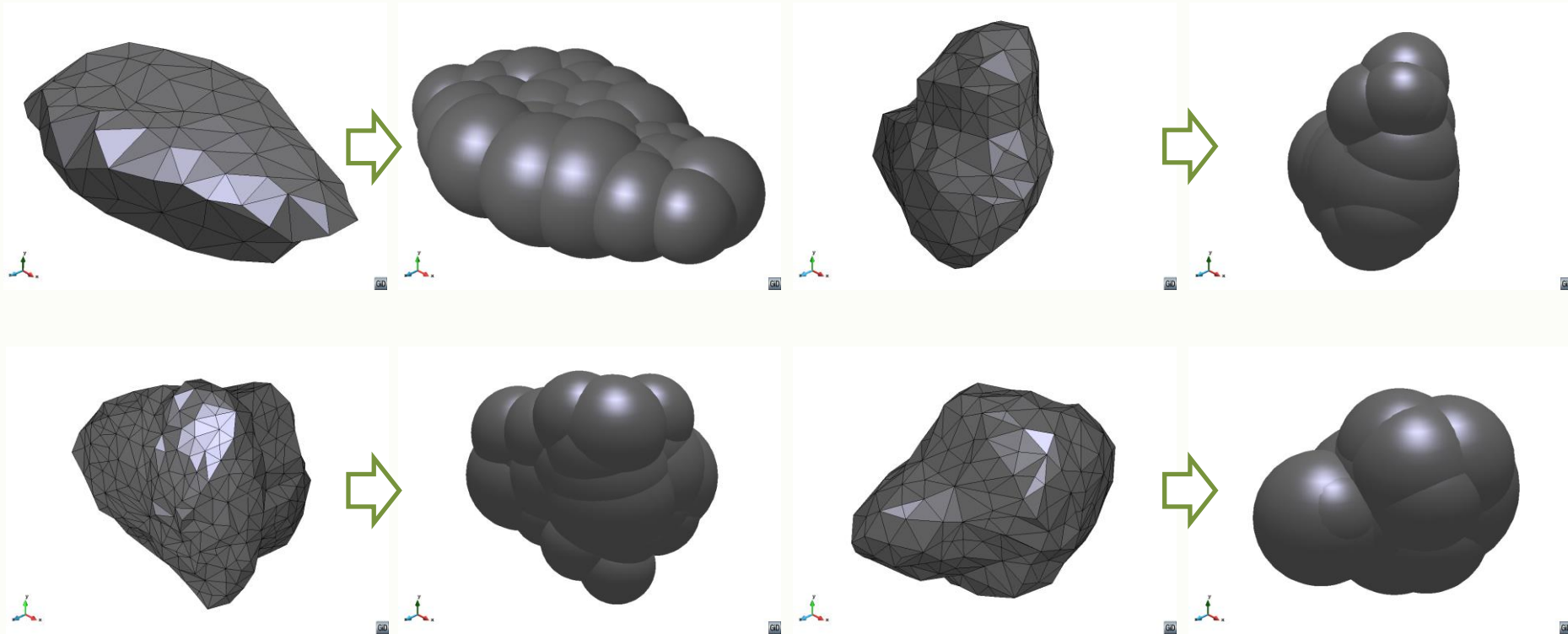
TEST RESULTS

Lateral resistance test:



DIFFERENT PARTICLES SHAPE

Sphere clusters:



Sphere-Tree Construction Toolkit (<http://isg.cs.tcd.ie/spheretree/>)

DIFFERENT PARTICLE SHAPES

Triaxial test:

Diameter = 0.305 m

Height = 0.61 m

Confining pressure = 68.9 kPa

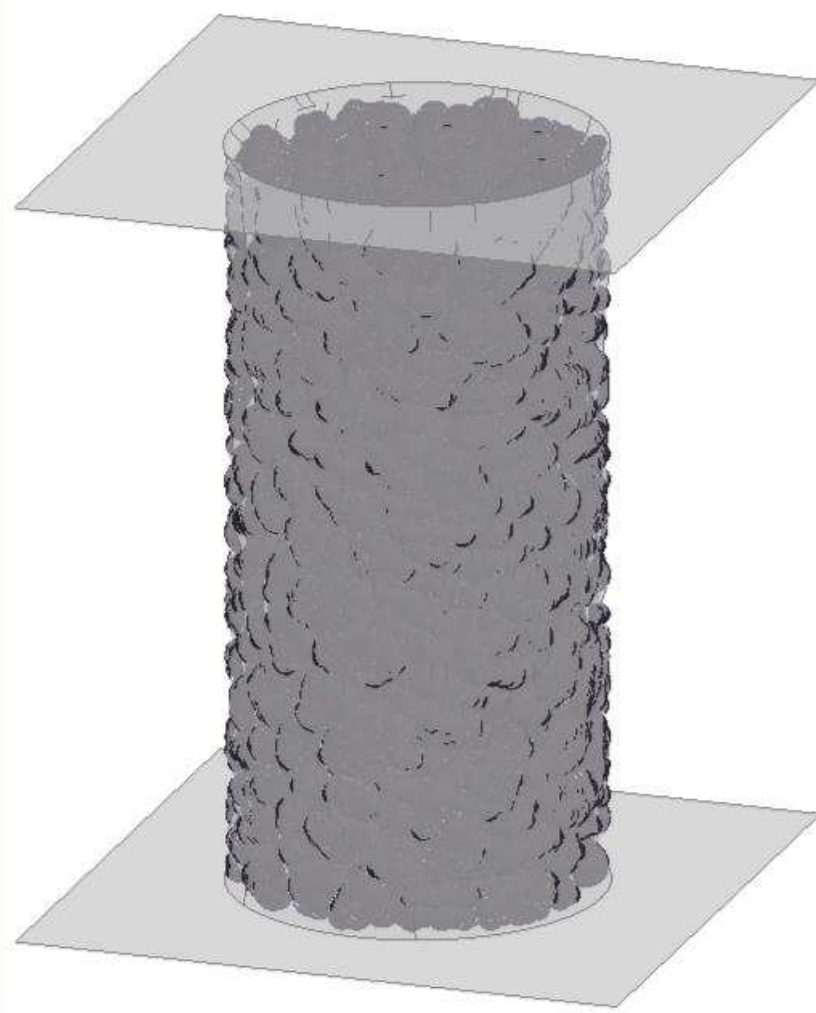
Shear velocity = 0.038 m/s



Quian et al. (2013) Triaxial compression test device - University of Illinois

DIFFERENT PARTICLE SHAPES

Triaxial test:



Ballast properties

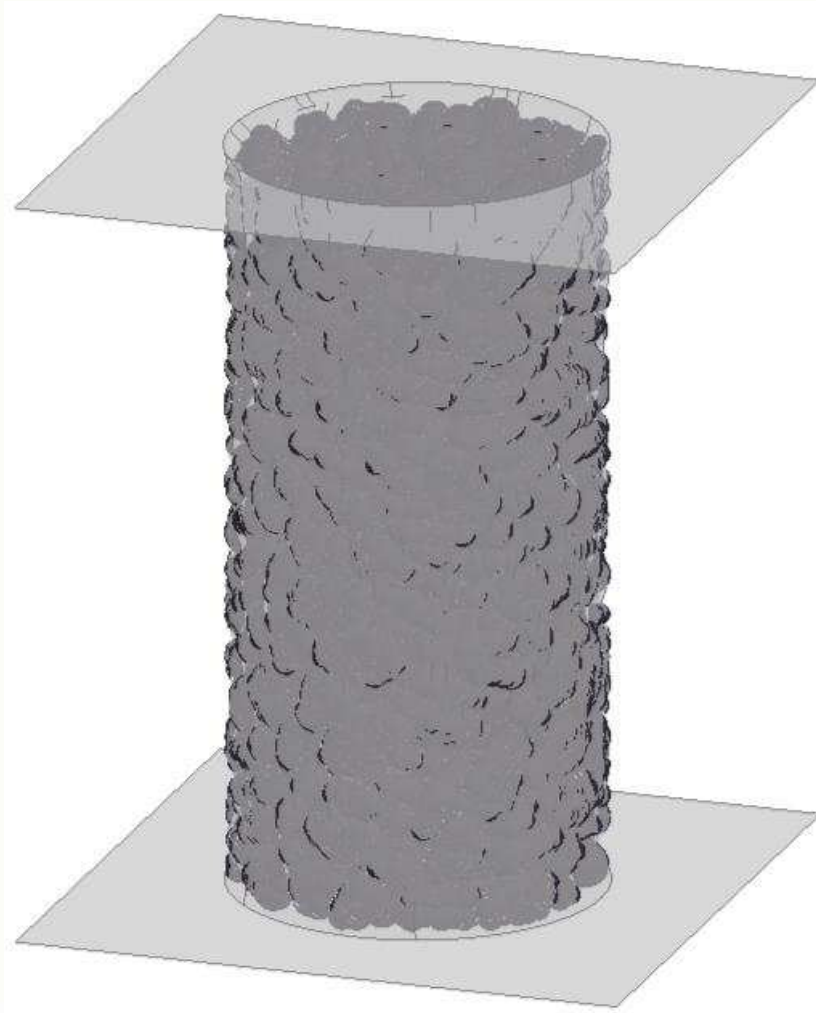
Density (kg/m^3)	2700
Young Modulus (Pa)	$5.1\text{e}9$
Poisson ratio	0.18
Mean diameter (m)	0.05
Friction coeff.	0.4
Friction coeff. ballast/membrane	0.0
Friction coeff. ballast/actuators	0.268
Restitution coeff.	0.4

Membrane properties

Young Modulus (Pa)	$1.5\text{e}6$
Poisson ratio	0.45
Thickness (m)	0.0023
Penalty factor (γ)	100

DIFFERENT PARTICLE SHAPES

Triaxial test:



Ballast properties

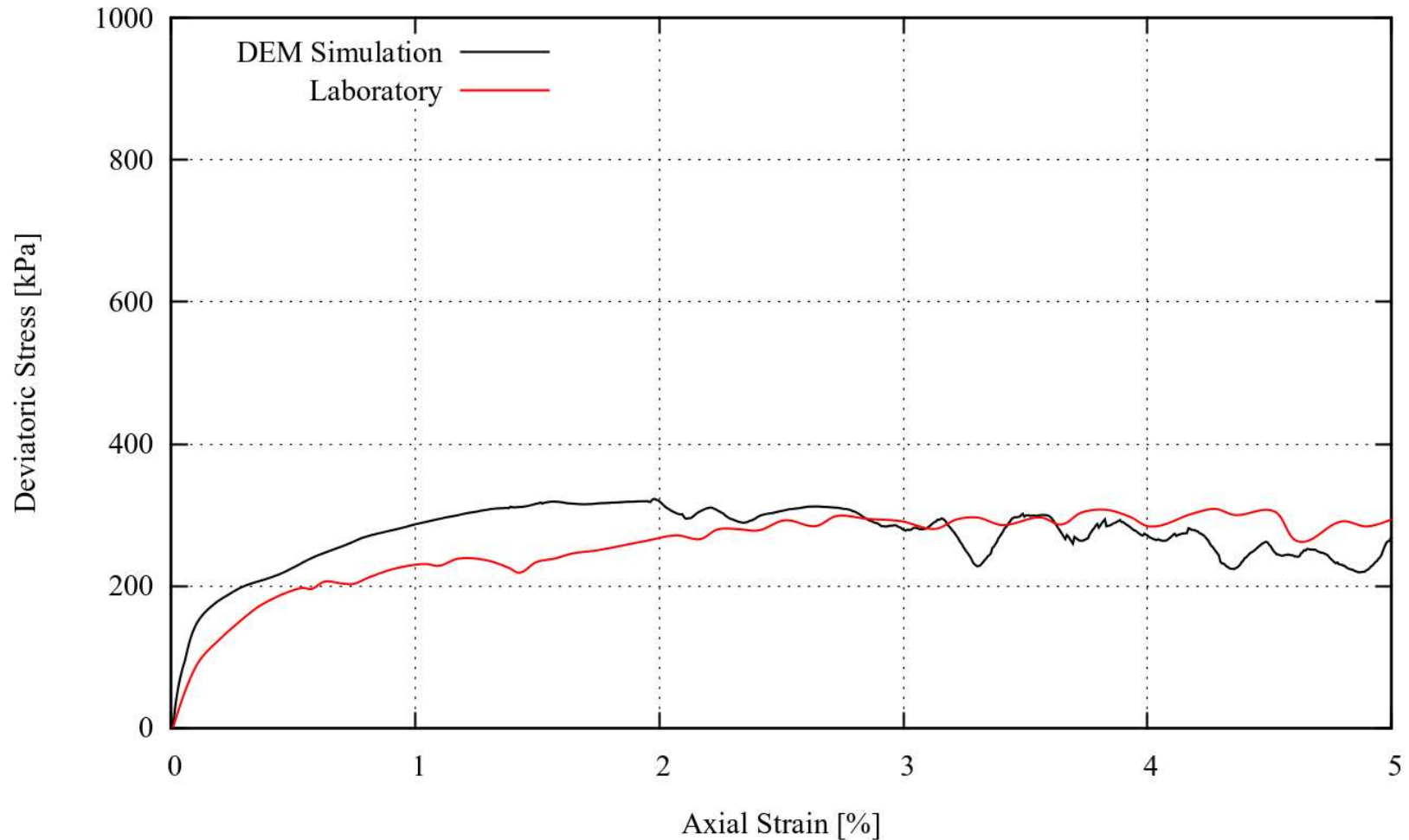
Density (kg/m^3)	2700
Young Modulus (Pa)	$5.1\text{e}9$
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Membrane properties

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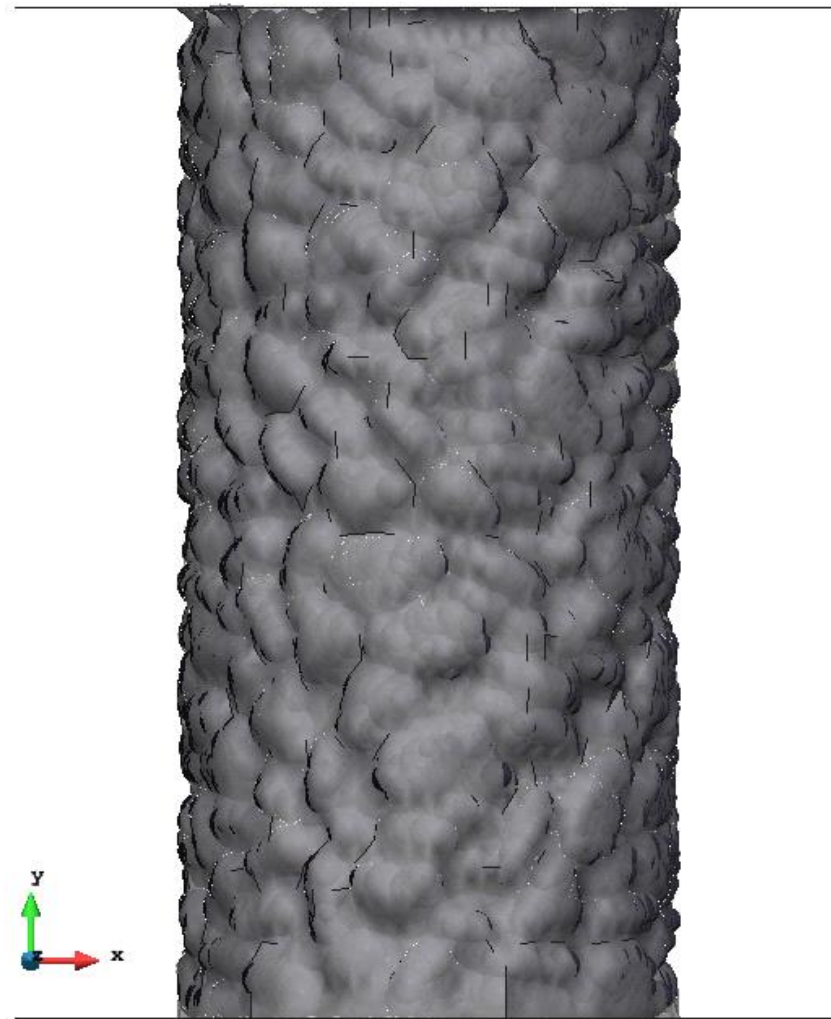
DIFFERENT PARTICLE SHAPES

Triaxial test:



DIFFERENT PARTICLE SHAPES

Triaxial test:



CONCLUSIONS

- **The DEM is an appropriate method for the calculation of ballast aggregates**
- **Rolling friction is useful for calculations with a great amount of material**
- **Material stiffness is a key property when measuring deformations**
- **Particle packing is an important variable**
- **Sphere clusters are a good approach to represent real geometries with low computational cost, but more validation work should be developed**

THANK YOU FOR YOUR ATTENTION



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Fernando Salazar (fsalazar@cimne.upc.edu)
Eugenio Oñate (onate@cimne.upc.edu)